

# CS 243

## Lecture 11

### Binary Decision Diagrams (BDDs) in Pointer Analysis

1. Datalog → BDD
2. BDDs
3. Context-Sensitive Pointer Analysis
4. Performance of BDD Algorithms

Readings: Chapter 12

Advanced Compilers

M. Lam & J. Whaley

## Automatic Analysis Generation



Programmer:  
Security analysis  
in 10 lines

PQL

Compiler writer:  
Ptr analysis  
in 10 lines

Datalog

**bddb**  
(**BDD-based**  
**deductive database**)  
with  
Active Machine Learning

1000s of lines  
1 year tuning

BDD operations

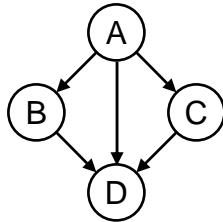
BDD: 10,000s-lines library

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# 1. Datalog $\rightarrow$ BDDs

- Example



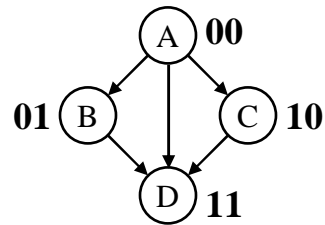
calls(A,B)  
 calls(A,C)  
 calls(A,D)  
 calls(B,D)  
 calls(C,D)

## Call Graph Relation

$x_1$	$x_2$	$x_3$	$x_4$	f
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

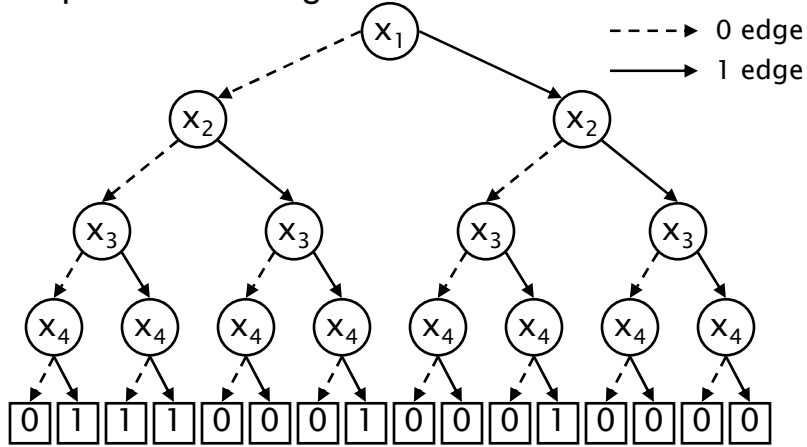
- Relation expressed as a binary function.

- A=00, B=01, C=10, D=11



# Binary Decision Diagrams (Bryant, 1986)

- Graphical encoding of a truth table.

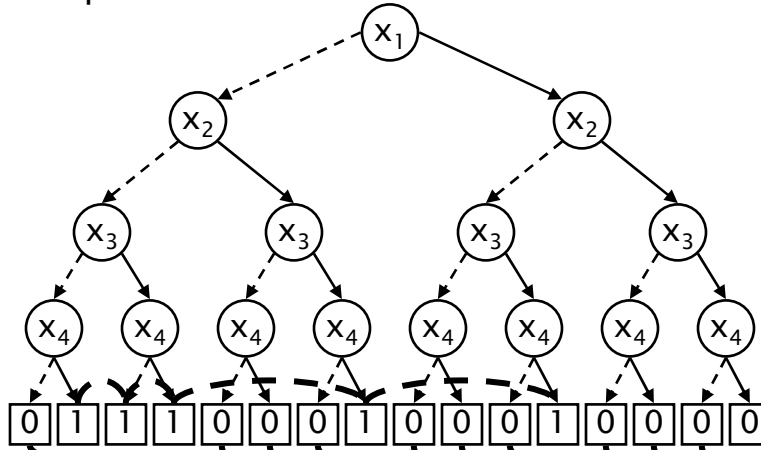


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# Binary Decision Diagrams

- Collapse redundant nodes.

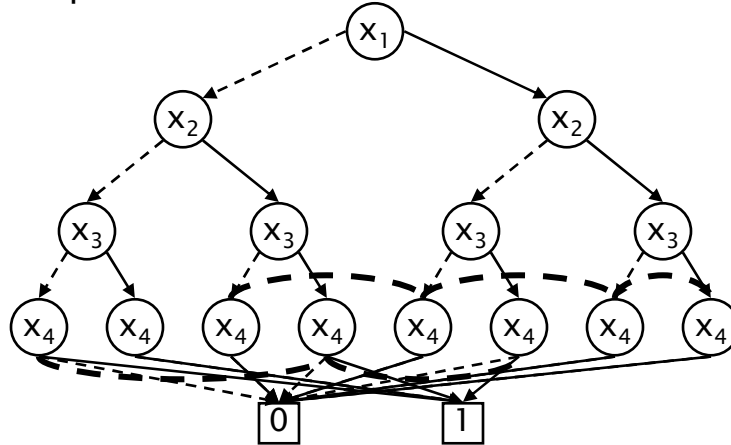


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# Binary Decision Diagrams

- Collapse redundant nodes.

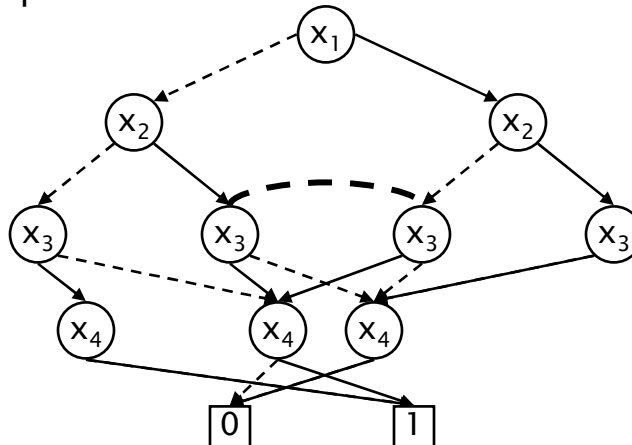


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# Binary Decision Diagrams

- Collapse redundant nodes.

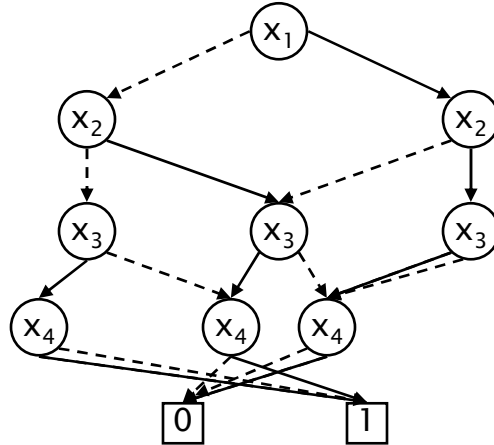


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# Binary Decision Diagrams

- Collapse redundant nodes.

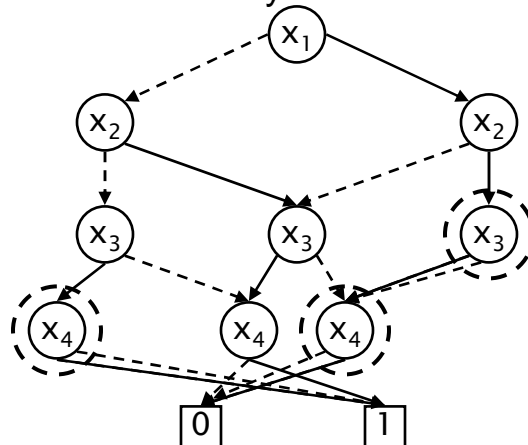


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# Binary Decision Diagrams

- Eliminate unnecessary nodes.

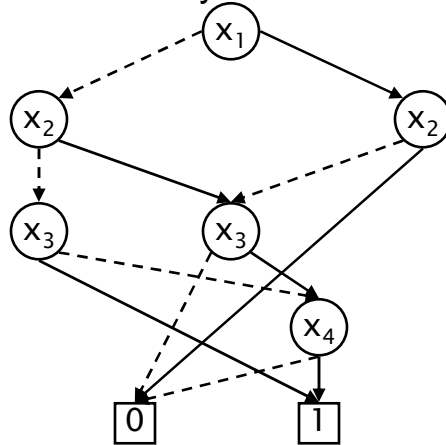


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# Binary Decision Diagrams

- Eliminate unnecessary nodes.



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## Datalog $\rightarrow$ BDDs

Datalog	BDDs
Relations	Boolean functions
Relation ops: $\bowtie, \cup, \text{select}, \text{project}$	Boolean function ops: $\wedge, \vee, \neg, \sim$
Relation at a time	Function at a time
Semi-naïve evaluation	Incrementalization
Fixed-point	Iterate until stable

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## 2. Binary Decision Diagrams

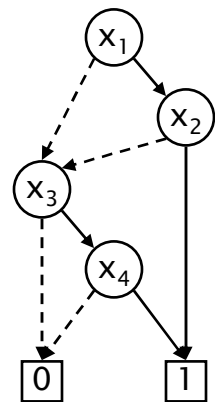
- Represent tiny and huge relations compactly
- Size depends on redundancy
  - Similar contexts have similar numberings
  - Variable ordering in BDDs

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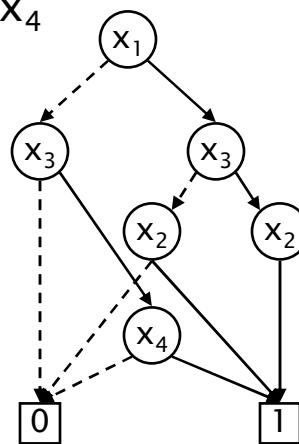
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### BDD Variable Order is Important!

$$x_1x_2 + x_3x_4$$



$$x_1 < x_2 < x_3 < x_4$$

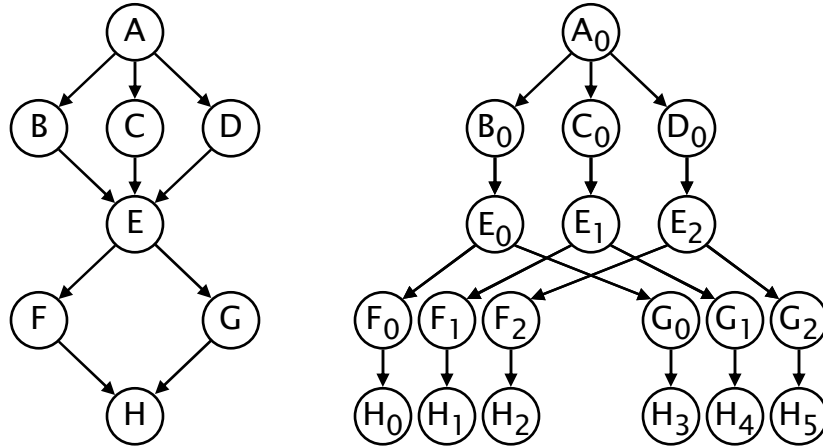


$$x_1 < x_3 < x_2 < x_4$$

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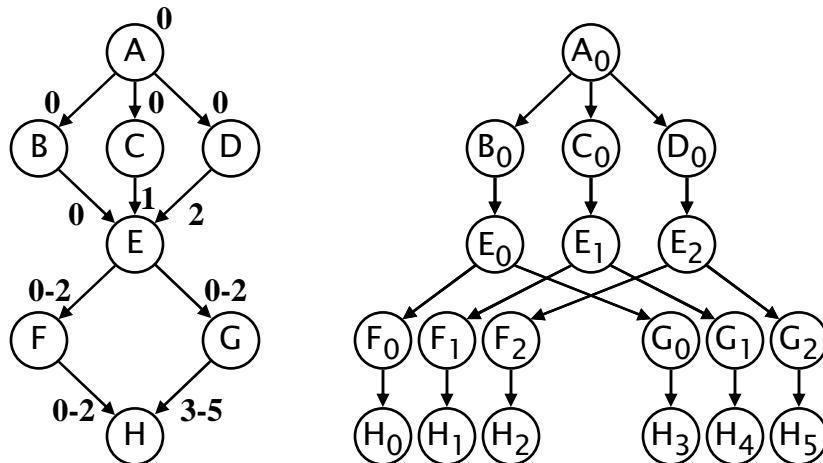
## Expanded Call Graph



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## Numbering Clones



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### 3. Context-Sensitive Pointer Analysis Algorithm

1. First, do context-insensitive pointer analysis to get call graph.
2. Number clones.
3. Do context-insensitive algorithm on the cloned graph.
  - Results explicitly generated for every clone.
  - Individual results retrievable with Datalog query.

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### 4. Performance of BDD Algorithm

- Direct implementation
  - Does not finish even for small programs
  - > 3000 lines of code
- Requires tuning for about 1 year
- Easy to make mistakes
  - Mistakes found months later

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## An Adventure in BDDs

- Context-sensitive numbering scheme
  - Modify BDD library to add special operations.
  - Can't even analyze small programs. *Time: ∞*
- Improved variable ordering
  - Group similar BDD variables together.
  - Interleave equivalence relations.
  - Move common subsets to edges of variable order. *Time: 40h*
- Incrementalize outermost loop
  - Very tricky, many bugs. *Time: 36h*
- Factor away control flow, assignments
  - Reduces number of variables *Time: 32h*

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## An Adventure in BDDs

- Exhaustive search for best BDD order
  - Limit search space by not considering intradomain orderings. *Time: 10h*
- Eliminate expensive rename operations
  - When rename changes relative order, result is not isomorphic. *Time: 7h*
- Improved BDD memory layout
  - Preallocate to guarantee contiguous. *Time: 6h*
- BDD operation cache tuning
  - Too small: redo work, too big: bad locality
  - Parameter sweep to find best values. *Time: 2h*

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## An Adventure in BDDs

- Simplified treatment of exceptions
  - Reduce number of vars, iterations necessary for convergence. *Time: 1h*
- Change iteration order
  - Required redoing much of the code. *Time: 48m*
- Eliminate redundant operations
  - Introduced subtle bugs. *Time: 45m*
- Specialized caches for different operations
  - Different caches for and, or, etc. *Time: 41m*

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## An Adventure in BDDs

- Compacted BDD nodes
  - 20 bytes → 16 bytes *Time: 38m*
- Improved BDD hashing function
  - Simpler hash function. *Time: 37m*
- Total development time: 1 year
  - 1 year per analysis?!?
- Optimizations obscured the algorithm.
- Many bugs discovered, maybe still more.

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## Variable Numbering: Active Machine Learning

- Must be determined dynamically
- Limit trials with properties of relations
- Each trial may take a long time
- Active learning:  
select trials based on uncertainty
- Several hours
- Comparable to exhaustive for small apps

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## Optimizations in bddbddb

- Algorithmic
  - Clever context numbering to exploit similarities
- Query optimizations
  - Magic-set transformation
  - semi-naïve evaluation
- Compiler optimizations
  - Redundancy elimination, liveness analysis
- BDD optimizations
  - Active machine learning
- BDD library extensions and turning

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Datalog

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BDD operations

**bddbddb**  
(**BDD**-based  
deductive **database**)  
with  
Active Machine Learning

BDD: 10,000s-lines library

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## Software

- System is publicly available at:  
<http://bddbddb.sourceforge.net>
- A ready-to-use version is available as a  
LivePC at <http://www.moka5.com>

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